



Érdekességek

Bizonyítás

```
calculus =  
  {ForAll[f, integral[derivative[f]] == f], ForAll[f, derivative[integral[f]] == f],  
   ForAll[{f, g}, derivative[product[f, g]] ==  
     sum[product[f, derivative[g]], product[g, derivative[f]]],  
   ForAll[{f, g}, derivative[sum[f, g]] == sum[derivative[f], derivative[g]]]}  
  
proof = FindEquationalProof[ForAll[{f, g},  
  sum[integral[product[f, derivative[g]]],  
  integral[product[g, derivative[f]]] == product[f, g]],  
  calculus]
```

Out[]:= ProofObject[  Logic: EquationalLogic Steps: 11
Theorem: $\forall_{\{f,g\}} \text{sum}[\text{integral}[\text{product}[f, \langle\langle 1 \rangle\rangle], \langle\langle 1 \rangle\rangle] == \langle\langle 1 \rangle\rangle]$]

In[]:= proof["ProofNotebook"]



Axiom 1

We are given that:

$$x1 == \text{derivative}[\text{integral}[x1]]$$

Axiom 2

We are given that:

$$x1 == \text{integral}[\text{derivative}[x1]]$$

Axiom 3

We are given that:

$$\text{derivative}[\text{sum}[x1, x2]] == \text{sum}[\text{derivative}[x1], \text{derivative}[x2]]$$

Axiom 4

We are given that:

$$\text{derivative}[\text{product}[x1, x2]] == \text{sum}[\text{product}[x1, \text{derivative}[x2]], \text{product}[x2, \text{derivative}[x1]]$$

Hypothesis 1

We would like to show that:

$$\text{sum}[\text{integral}[\text{product}[f, \text{derivative}[g]]], \text{integral}[\text{product}[g, \text{derivative}[f]]] == \text{product}[f$$

Critical Pair Lemma 1

The following expressions are equivalent:

$$\text{derivative}[\text{sum}[\text{integral}[x1], x2]] == \text{sum}[x1, \text{derivative}[x2]]$$

PROOF

Note that the input for the rule:

$\text{sum}[\text{derivative}[x1_], \text{derivative}[x2_]] \rightarrow \text{derivative}[\text{sum}[x1, x2]]$

contains a subpattern of the form:

$\text{derivative}[x1_]$

which can be unified with the input for the rule:

$\text{derivative}[\text{integral}[x1_]] \rightarrow x1$

where these rules follow from Axiom 3 and Axiom 1 respectively.

Critical Pair Lemma 2

The following expressions are equivalent:

$\text{sum}[\text{integral}[x1], x2] == \text{integral}[\text{sum}[x1, \text{derivative}[x2]]]$

PROOF

Note that the input for the rule:

$\text{integral}[\text{derivative}[x1_]] \rightarrow x1$

contains a subpattern of the form:

$\text{derivative}[x1_]$

which can be unified with the input for the rule:

$\text{derivative}[\text{sum}[\text{integral}[x1_], x2_]] \rightarrow \text{sum}[x1, \text{derivative}[x2]]$

where these rules follow from Axiom 2 and Critical Pair Lemma 1 respectively.

Critical Pair Lemma 3

The following expressions are equivalent:

$\text{sum}[\text{integral}[x1], \text{integral}[x2]] == \text{integral}[\text{sum}[x1, x2]]$

PROOF

Note that the input for the rule:

$\text{integral}[\text{sum}[x1_ , \text{derivative}[x2_]]] \rightarrow \text{sum}[\text{integral}[x1], x2]$

contains a subpattern of the form:

$\text{derivative}[x2_]$

which can be unified with the input for the rule:

$\text{derivative}[\text{integral}[x1_]] \rightarrow x1$

where these rules follow from Critical Pair Lemma 2 and Axiom 1 respectively.

Substitution Lemma 1

It can be shown that:

$\text{integral}[\text{sum}[\text{product}[f, \text{derivative}[g]], \text{product}[g, \text{derivative}[f]]]] == \text{product}[f, g]$

PROOF

We start by taking Hypothesis 1, and apply the substitution:

$\text{sum}[\text{integral}[x1_], \text{integral}[x2_]] \rightarrow \text{integral}[\text{sum}[x1, x2]]$

which follows from Critical Pair Lemma 3.

Substitution Lemma 2

It can be shown that:

$\text{integral}[\text{derivative}[\text{product}[f, g]]] == \text{product}[f, g]$

PROOF

We start by taking Substitution Lemma 1, and apply the substitution:

$\text{sum}[\text{product}[x1_ , \text{derivative}[x2_]], \text{product}[x2_ , \text{derivative}[x1_]]] \rightarrow \text{derivative}[\text{product}[x1$

Out[]:=

which follows from Axiom 4.

Conclusion 1

We obtain the conclusion:

True

PROOF

Take Substitution Lemma 2, and apply the substitution:

integral[derivative[x1_]]→x1

which follows from Axiom 2.

Fordítás

```
In[ ]:= TextTranslation["Where is the library?", #] & /@ {"Russian", "German", "Spanish"}
```

```
Out[ ]:= {Где находится библиотека?,
          Wo befindet sich die Bibliothek?, ¿Dónde está la biblioteca?}
```

```
Export["transl.tex", %, "TeX"]
```

```
Out[ ]:= transl.tex
```

Értő olvasás

```
context = "The population of Paris in its
          administrative city limits was 2,241,346 in January 2014.
          Paris is the capital and most populous city of France, with
          a 2015 population of 2,229,621.
          By the 17th century, Paris had become one of Europe's major centres of
          finance, commerce, fashion, science,
          and the arts, a position that it retains still today";
questions = {"What is Paris?",
            "When did Paris have a population of 2.24 million?",
            "Why is Paris famous in Europe?";

res =
  Thread[questions -> FindTextualAnswer[context, questions, 1, "HighlightedSentence"]]
  // TableForm

"What is Paris?" ->
  {"Paris is " the capital and most populous city of France ", }
  with a 2015 population of 2,229,621."

"When did Paris have a population of 2.24 million?" ->
  {"The population of Paris in its administrative city limits was 2,241,346 in " January

"Why is Paris famous in Europe?" ->
  {"By the 17th century, Paris had become one of Europe's
  " major centres of finance, commerce, fashion, science, and the arts ",
  a position that it retains still today"
```