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(*** Wolfram Notebook File ***)

(* http://www.wolfram.com/nb *)

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NotebookFileLineBreakTest

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NotebookDataPosition[158, 7]

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WindowFrame->Normal*)

(* Beginning of Notebook Content *)

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Let $a_0=1$, $a_1=2$, and $a_n=4a_{n-1}-a_{n-2}$ for $n \geq 2$. Find an odd \ prime factor of a_{2015} .

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